

EBBING - GAMMON

General
Chemistry

ELEVENTH EDITION

The Gaseous State

➤ Gas Laws

Most substances composed of small molecules are gases under normal conditions or else are easily vaporized liquids

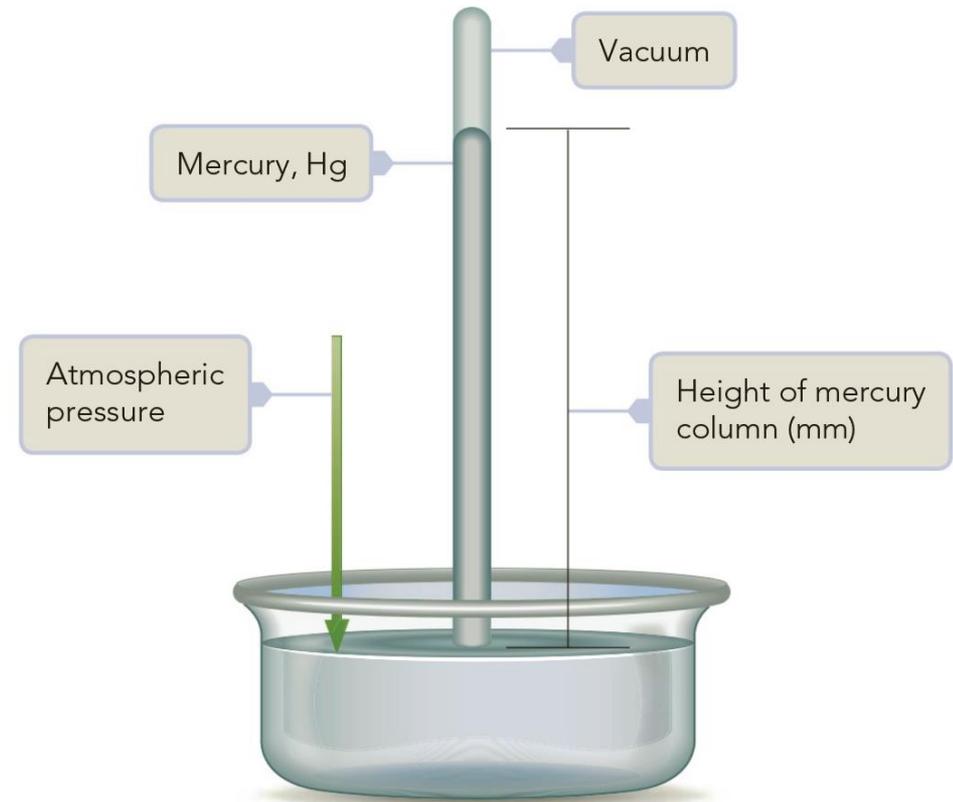
Table 5.1 Properties of Selected Gases

Name	Formula	Color	Odor	Toxicity
Ammonia	NH ₃	Colorless	Penetrating	Toxic
Carbon dioxide	CO ₂	Colorless	Odorless	Nontoxic
Carbon monoxide	CO	Colorless	Odorless	Very toxic
Chlorine	Cl ₂	Pale green	Irritating	Very toxic
Hydrogen	H ₂	Colorless	Odorless	Nontoxic
Hydrogen sulfide	H ₂ S	Colorless	Foul	Very toxic
Methane	CH ₄	Colorless	Odorless	Nontoxic
Nitrogen dioxide	NO ₂	Red-brown	Irritating	Very toxic

5.1 Gas Pressure and Its Measurement

Pressure is defined as *the force exerted per unit area of surface*

- ✓ Force = mass \times constant acceleration of gravity
- ✓ SI unit of pressure, $\text{kg}/(\text{m}\cdot\text{s}^2)$, is given the name **pascal (Pa)**
- ✓ A **barometer** is a device for measuring the pressure of the atmosphere
- ✓ A **manometer**, a device that measures the pressure of a gas or liquid in a vessel



mercury barometer

✓ Pressure of a coin (9.3 mm in radius and 2.5 g)

$$\text{Force} = \text{mass} \times g = (2.5 \times 10^{-3} \text{ kg}) \times (9.81 \text{ m/s}^2)$$

$$\text{Area} = \pi \times (\text{radius})^2 = 3.14 \times (9.3 \times 10^{-3} \text{ m})^2$$

$$\text{Pressure} = \frac{\text{force}}{\text{area}} = \frac{2.5 \times 10^{-2} \text{ kg}\cdot\text{m/s}^2}{2.7 \times 10^{-4} \text{ m}^2} = 93 \text{ kg}/(\text{m}\cdot\text{s}^2) = 93 \text{ Pa}$$

✓ The general relationship between the pressure P and the height h of a liquid column in a barometer or manometer is:

$$P = \rho gh$$

Table 5.2 Important Units of Pressure

Unit	Relationship or Definition
Pascal (Pa)	$\text{kg}/(\text{m}\cdot\text{s}^2)$
Atmosphere (atm)	$1 \text{ atm} = 1.01325 \times 10^5 \text{ Pa} \approx 101 \text{ kPa}$
mmHg, or torr	$760 \text{ mmHg} = 1 \text{ atm}$
Bar	$1.01325 \text{ bar} = 1 \text{ atm}$

Example 5.1 Converting Units of Pressure

(Q) The pressure of a gas in a flask is measured to be 797.7 mmHg. What is this pressure in pascals and atmospheres?

Solution Conversion to pascals:

$$797.7 \text{ mmHg} \times \frac{1.01325 \times 10^5 \text{ Pa}}{760 \text{ mmHg}} = \mathbf{1.064 \times 10^5 \text{ Pa}}$$

Conversion to atmospheres:

$$797.7 \text{ mmHg} \times \frac{1 \text{ atm}}{760 \text{ mmHg}} = \mathbf{1.050 \text{ atm}}$$

➤ 5.2 Empirical Gas Laws

➤ Boyle's Law: Relating Volume and Pressure

Boyle's law:

$PV = \text{constant}$ (for a given amount of gas at fixed temperature)

the volume of a sample of gas at a given temperature varies inversely with the applied pressure. That is, $V \propto 1/P$, where V is the volume, P is the pressure,

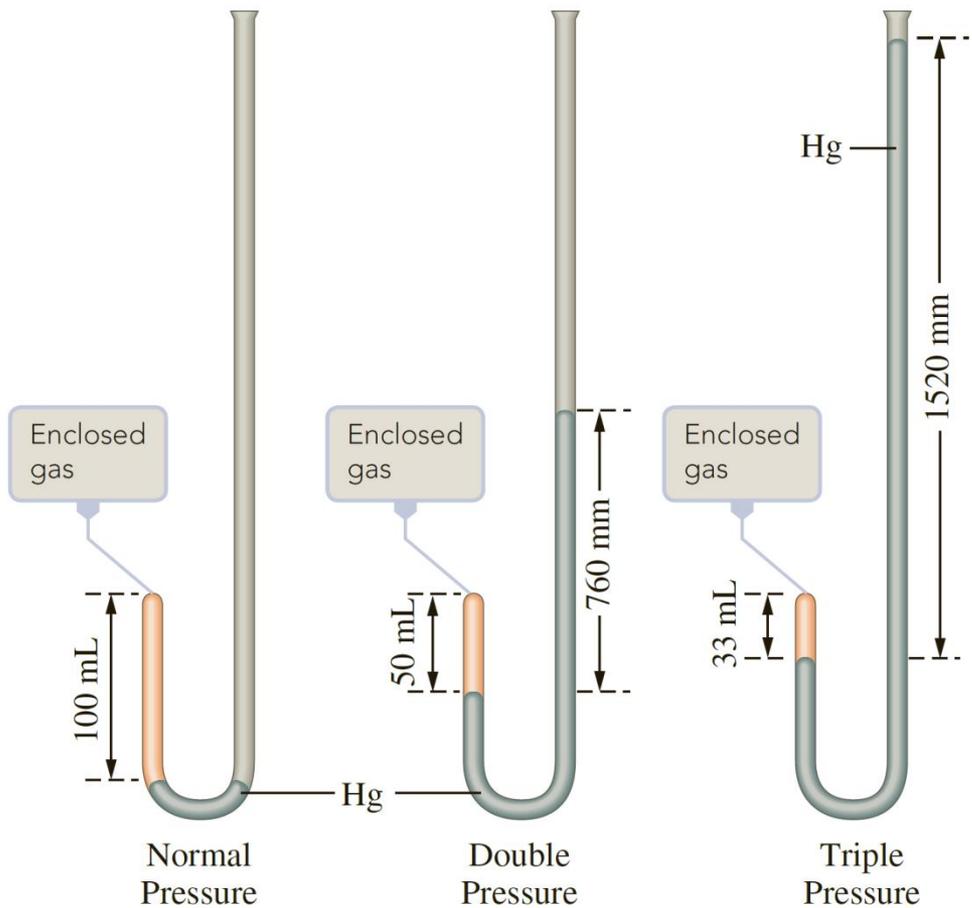


Table 5.3 Pressure–Volume Data for 1.000 g O_2 at $0^\circ C$

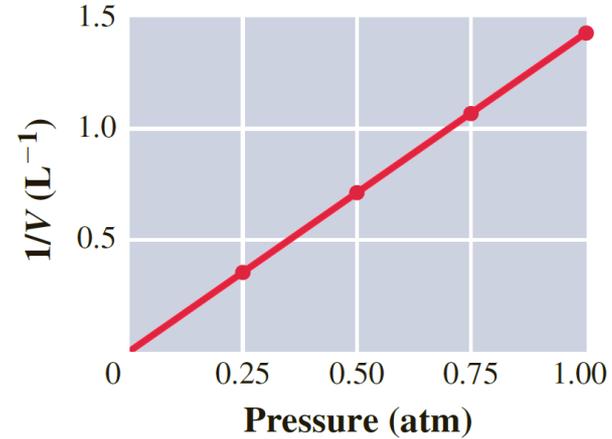
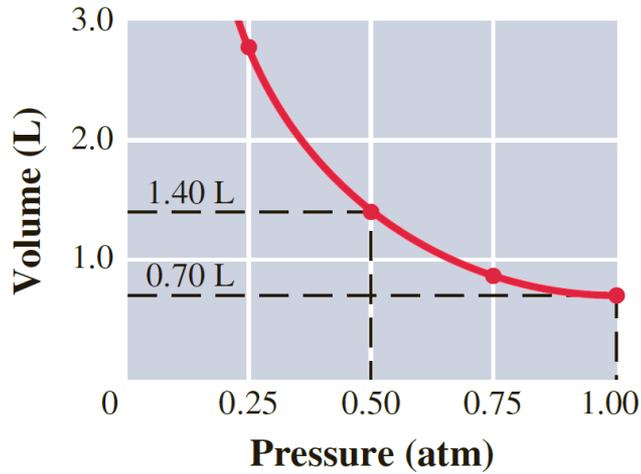
	P (atm)	V (L)	PV
Increasing pressure ↓	0.2500	2.801	0.7002
	0.5000	1.400	0.7000
	0.7500	0.9333	0.7000
	1.000	0.6998	0.6998
	2.000	0.3495	0.6990
↑ Increasing volume	3.000	0.2328	0.6984
	4.000	0.1744	0.6976
	5.000	0.1394	0.6970

➤ **Boyle's experiment:**

The volume of the gas at normal atmospheric pressure (760 mmHg) is 100 mL. When the pressure is doubled by adding 760 mm of mercury, the volume is halved (to 50 mL).

Tripling the pressure decreases the volume to one-third of the original (to 33 mL).

$$PV = \text{constant} \rightarrow P_1V_1 = P_2V_2$$



(Q) A volume of air occupying 12.0 dm³ at 98.9 kPa is compressed to a pressure of 119.0 kPa. The temperature remains constant. What is the new volume?

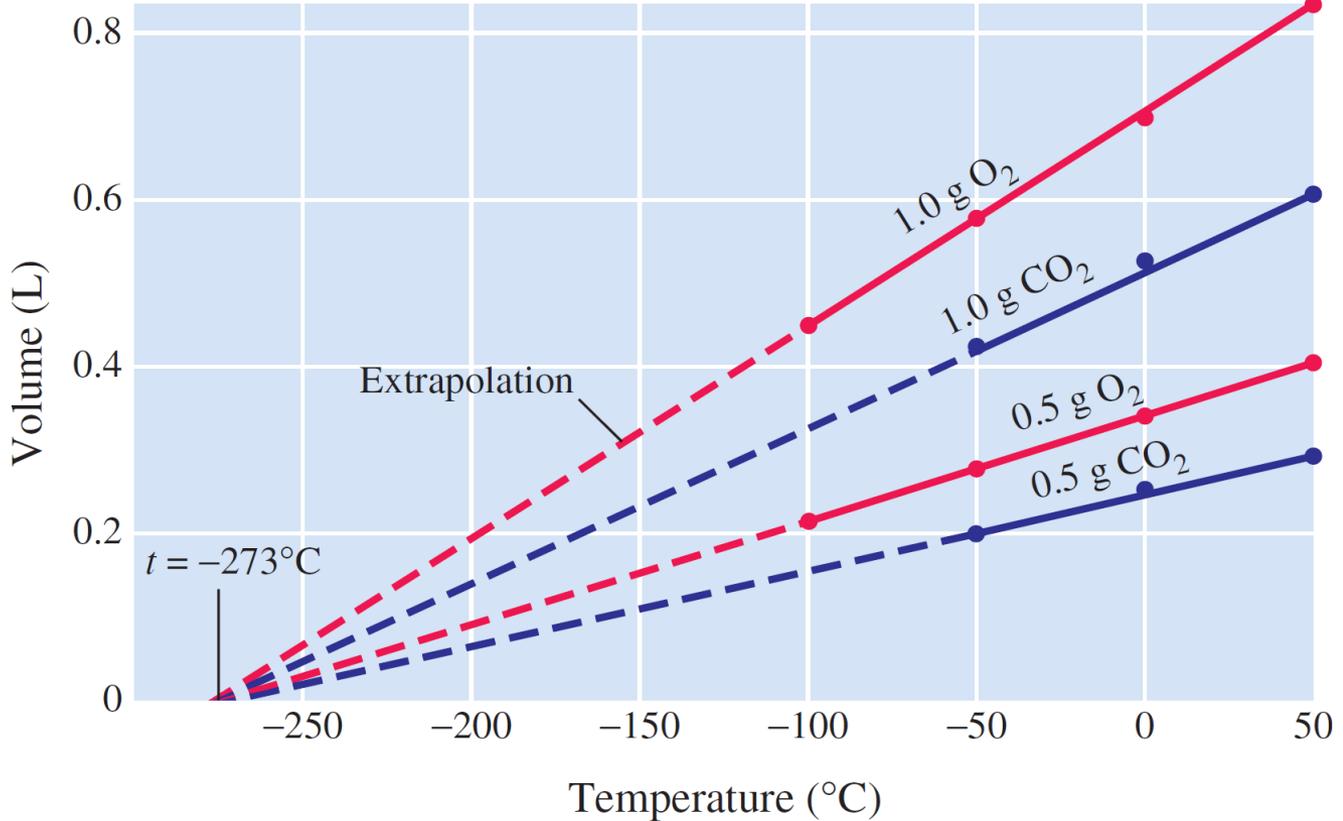
$$P_i V_i = P_f V_f$$

$$V_f = V_i \times \frac{P_i}{P_f} = 12.0 \text{ dm}^3 \times \frac{98.9 \text{ kPa}}{119.0 \text{ kPa}} = \mathbf{9.97 \text{ dm}^3}$$

➤ Charles's Law: Relating Volume and Temperature

$$\frac{V}{T} = \text{constant} \quad (\text{for a given amount of gas at a fixed pressure})$$

$$\frac{V_f}{T_f} = \frac{V_i}{T_i}$$



Exercise 5.3 If you expect a chemical reaction to produce 4.38 dm³ of oxygen, O₂, at 19°C and 101 kPa, what will be the volume at 25°C and 101 kPa?

First, convert the temperatures to the Kelvin.

$$T_i = (19 + 273) = 292 \text{ K}$$

$$T_f = (25 + 273) = 298 \text{ K}$$

Apply Charles's law

$$V_f = V_i \times \frac{T_f}{T_i} = 4.38 \text{ dm}^3 \times \frac{298 \text{ K}}{292 \text{ K}} = 4.470 = 4.47 \text{ dm}^3$$

➤ Combined Gas Law: Relating Volume, Temperature, and Pressure

✓ Boyle's law ($V \propto 1/P$) and Charles's law ($V \propto T$) can be combined to:

$$V \propto T/P$$

$$V = \text{constant} \times \frac{T}{P} \quad \text{or} \quad \frac{PV}{T} = \text{constant} \quad (\text{for a given amount of gas})$$

$$\frac{P_f V_f}{T_f} = \frac{P_i V_i}{T_i}$$

(Q) A 39.8 mg sample of caffeine gives 10.1 cm³ of N₂ gas at 23°C and 746 mmHg. What is the volume of N₂ at 0°C and 760 mmHg?

$$T_i = (23 + 273) \text{ K} = 296 \text{ K}$$

$$T_f = (0 + 273) \text{ K} = 273 \text{ K}$$

$$V_f = V_i \times \frac{P_i}{P_f} \times \frac{T_f}{T_i} = 10.1 \text{ cm}^3 \times \frac{746 \text{ mmHg}}{760 \text{ mmHg}} \times \frac{273 \text{ K}}{296 \text{ K}} = \mathbf{9.14 \text{ cm}^3}$$

(Q) What will be the final pressure of a sample of nitrogen gas with a volume of 950. m³ at 745 torr and 25.0 °C if it is heated to 60.0 °C and given a final volume of 1150 m³?

Exercise 5.4

A balloon contains 5.41 dm³ of helium, He, at 24°C and 101.5 kPa. Suppose the gas in the balloon is heated to 35°C. If the helium pressure is now 102.8 kPa, what is the volume of the gas?

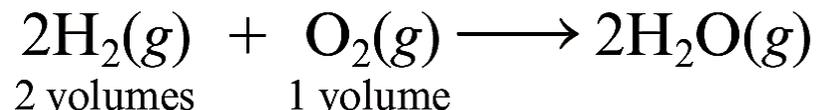
$$T_i = (24 + 273) = 297 \text{ K}$$

$$T_f = (35 + 273) = 308 \text{ K}$$

$$V_f = V_i \times \frac{P_i}{P_f} \times \frac{T_f}{T_i} = 5.41 \text{ dm}^3 \times \frac{101.5 \text{ kPa}}{102.8 \text{ kPa}} \times \frac{308 \text{ K}}{297 \text{ K}} = 5.539 = 5.54 \text{ dm}^3$$

➤ Avogadro's Law: Relating Volume and Amount

- ✓ French chemist Joseph Louis Gay-Lussac concluded from experiments on gas reactions that:
the volumes of reactant gases at the same pressure and temperature are in ratios of small whole numbers (*the law of combining volumes*).



✓ **Avogadro's law:**

equal volumes of any two gases at the same temperature and pressure contain the same number of molecules.

- ✓ volume of **one mole** of gas is called the molar gas volume, V_m .

Avogadro's law:

$V_m =$ specific constant (=22.4 L/mol at STP)
(depending on T and P but independent of the gas)

STP = Standard Temperature and Pressure (0°C and 1 atm)

➤ 5.3 The Ideal Gas Law

$$PV = nRT$$

(Q) How many grams of oxygen are there in a 50.0-L gas cylinder at 21°C when the oxygen pressure is 15.7 atm?

Exercise 5.6

What is the pressure in a 50.0-L gas cylinder that contains 3.03 kg of oxygen, O₂, at 23°C?

(Q) Calculate the volume (in L) occupied by 7.40 g of NH₃ at STP

$$\begin{aligned} V &= 7.40 \text{ g NH}_3 \times \frac{1 \text{ mol NH}_3}{17.03 \text{ g NH}_3} \times \frac{22.41 \text{ L}}{1 \text{ mol NH}_3} \\ &= 9.74 \text{ L} \end{aligned}$$

➤ Gas Density; Molecular-Weight Determination

$$PM_m = dRT$$

d is the density of the gas in g/L

(Q) What is the density of oxygen, O₂, in grams per liter at 25°C and 0.850 atm?

$$d = PM_m/RT = (0.85 \times 32) / (0.082 \times 298) = 1.11 \text{ g/L}$$

Exercise 5.8 A sample of a gaseous substance at 25°C and 0.862 atm. has a density of 2.26 g/L. What is the molecular weight of the substance?

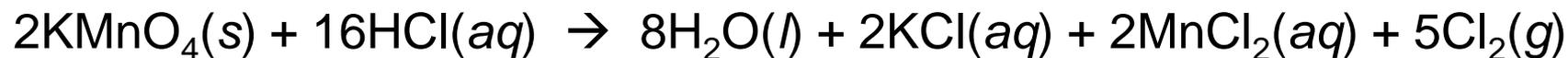
$$M_m = dRT/P = (2.26 \times 0.082 \times 298) / 0.862 = 64.1 \text{ g/mol}$$

5.4 Stoichiometry Problems Involving Gas Volumes



Calculate the volume of N_2 generated at 80°C and 823 mmHg by the decomposition of 60.0 g of NaN_3

Exercise 5.9 How many liters of chlorine gas, Cl_2 , can be obtained at 40°C and 787 mmHg from 9.41 g of hydrogen chloride, HCl , according to the following equation?

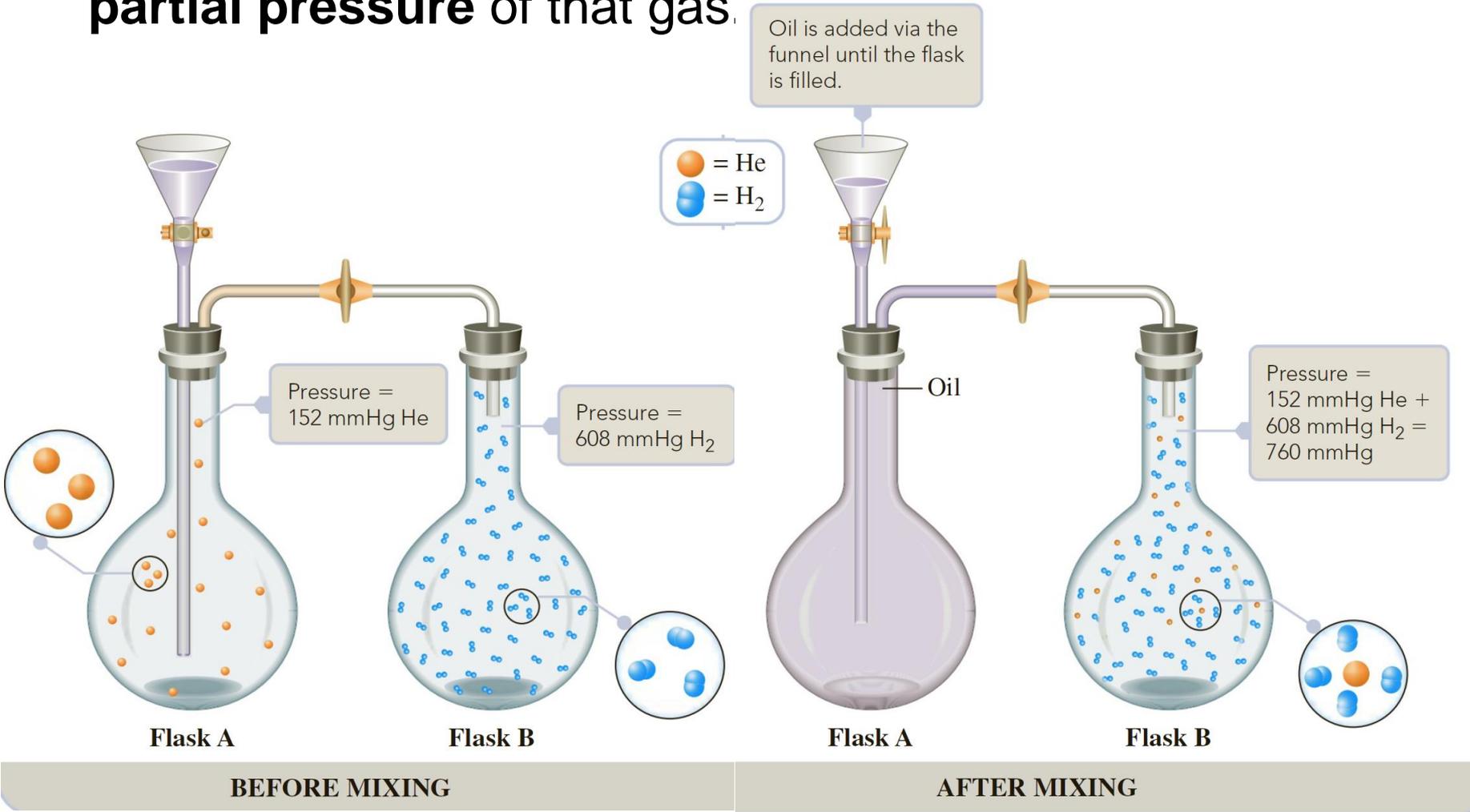


5.5 Gas Mixtures; Law of Partial Pressures

➤ Partial Pressures and Mole Fractions

✓ Dalton's law of partial pressures:

The pressure exerted by a particular gas in a mixture is the partial pressure of that gas.



Dalton's law of partial pressures:

$$P = P_A + P_B + P_C + \dots$$

✓ The individual partial pressures follow the ideal gas law. For component A, $P_A V = n_A RT$

$$\text{Mole fraction of } A = \frac{n_A}{n} = \frac{P_A}{P}$$

(Q) A 1.00-L sample of dry air at 25°C and 786 mmHg contains 0.925 g N₂, plus other gases including oxygen, argon, and carbon dioxide.

a. What is the partial pressure (in mmHg) of N₂ in the air sample?

b. What is the mole fraction and mole percent of N₂ in the

mixture? $0.925 \text{ g N}_2 \times \frac{1 \text{ mol N}_2}{28.0 \text{ g N}_2} = 0.0330 \text{ mol N}_2$

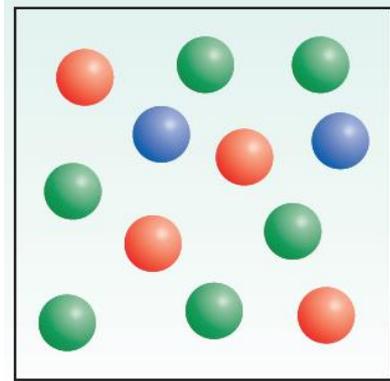
$$P_{\text{N}_2} = \frac{n_{\text{N}_2} RT}{V} = \frac{0.0330 \text{ mol} \times 0.0821 \text{ L}\cdot\text{atm}/(\text{K}\cdot\text{mol}) \times 298 \text{ K}}{1.00 \text{ L}} = 0.807 \text{ atm} (= 613 \text{ mmHg})$$

$$\text{Mole fraction of N}_2 = \frac{P_{\text{N}_2}}{P} = \frac{613 \text{ mmHg}}{786 \text{ mmHg}} = \mathbf{0.780}$$

Air contains **78.0 mole percent** of N₂.

(Q) Each of the color spheres represents a different gas molecule. Calculate the partial pressures of the gases if the total pressure is 2.6 atm.

$$\text{Mole fraction of } A = \frac{n_A}{n} = \frac{P_A}{P}$$



(Q) A mixture consists of 122 moles of N_2 , 137 moles of C_3H_8 , and 212 moles of CO_2 at 200 K in a 75.0 L container. What is the total pressure of the gas and the partial pressure of CO_2 ?

A. 46.4 atm, 20.9 atm

B. 103 atm, 26.7 atm

C. 103 atm, 46.4 atm

D. 103 atm, 29.9 atm

E. 46.4 atm, 46.4 atm

$$P_{\text{total}} = \frac{(471 \text{ moles})(0.0821 \text{ L atm mol}^{-1} \text{ K}^{-1})(200 \text{ K})}{75.0 \text{ L}}$$

$$P_{\text{total}} = 103 \text{ atm}$$

$$\text{mole fraction } CO_2 : \frac{212 \text{ moles } CO_2}{122 + 137 + 212 \text{ total}} = 0.450$$

$$P_{CO_2} = (\chi_{CO_2})(P_{\text{total}}) = (0.450)(103 \text{ atm})$$

$$P_{CO_2} = 46.4 \text{ atm}$$

(Q) A mixture of 250 mL of methane, CH_4 , at 35°C and 0.55 atm and 750 mL of propane, C_3H_8 , at 35°C and 1.5 atm was introduced into a 10.0 L container. What is the mole fraction of methane in the mixture?

A. 0.50

B. 0.11

C. 0.89

D. 0.25

E. 0.33

$$\text{Mole fraction of } A = \frac{n_A}{n} = \frac{P_A}{P}$$

$$P_{\text{CH}_4} = \frac{0.55 \text{ atm} \cdot 0.250 \text{ L}}{10.0 \text{ L}} = 0.0138 \text{ atm}$$

$$P_{\text{C}_3\text{H}_8} = \frac{1.5 \text{ atm} \cdot 0.750 \text{ L}}{10.0 \text{ L}} = 0.112 \text{ atm}$$

$$C_{\text{CH}_4} = \frac{0.0138 \text{ atm}}{0.0138 \text{ atm} + 0.112 \text{ atm}} = 0.110$$